







QUESTION BANK

WITH ANSWER KEY

& STRUCTURED EXPLANATION

CLASS 11
MATHEMATICS





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Let R_1 be a relation defined by

ARTHAM RESOURCES



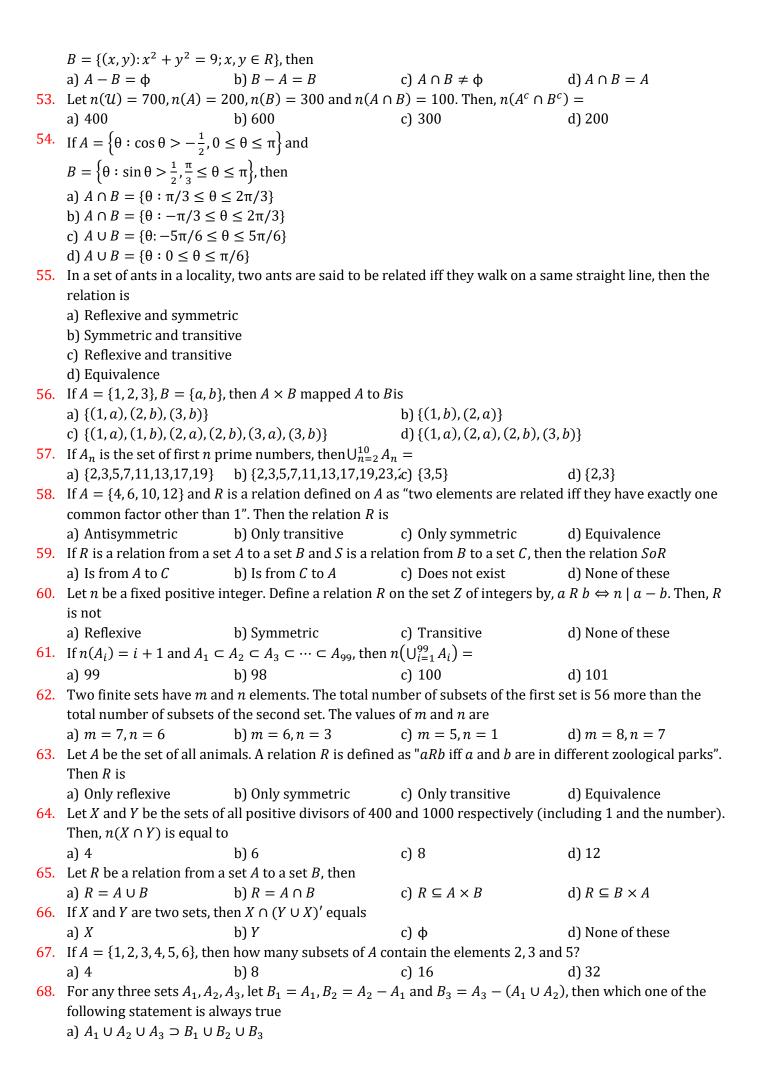
Class: 11 Mathematics
Competency-based Question Bank with Answer Key
& Structured Explanation

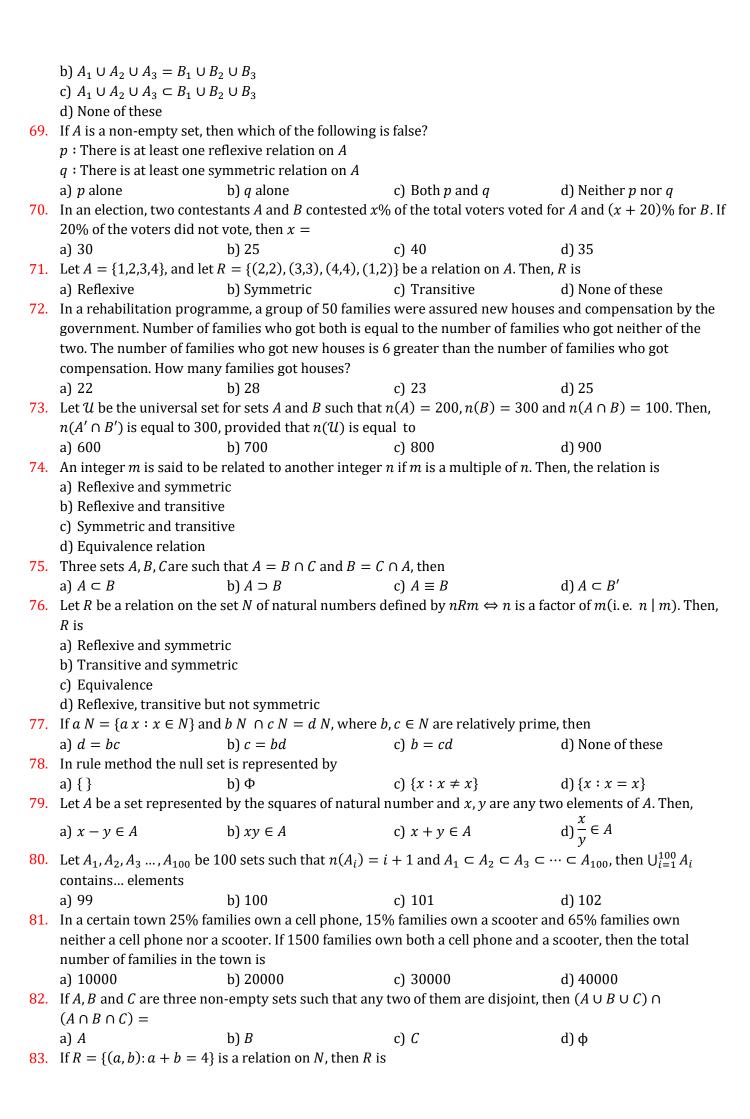
SETS

	$R_1 = \{(a, b) a \ge b, a, b \in R\}.$ Then, R_1 is										
	a) An equivalence relation on R										
	b) Reflexive, transitive but not symmetric										
	c) Symmetric, transitive but not reflexive										
	d) Neither transitive not reflexive but symmetric										
2.	On the set of human beings a relation <i>R</i> is defined as follows:										
	" aRb iff a and b have the same brother". Then R is										
	a) Only reflexive		c) Only transitive	d) Equivalence							
3.	•										
	In a class of 35 students, 17 have taken Mathematics, 10 have taken Mathematics but not Economics. If each student has taken either Mathematics or Economics or both, then the number of students who have										
	taken Economics but not Mathematics is										
	a) 7	b) 25	c) 18	d) 32							
4.	${n(n+1)(2n+1): n \in$	•	0) 10	., s_							
			c) $\{18k : k \in Z\}$	d) $\{24k : k \in 7\}$							
5.		$= \{2, 4, 6\}, C = \{3, 4, 6\}, t$		$u_j(21k \cdot k \in Z)$							
J.			c) {1, 4, 3}	d) None of these							
6.			lation R is defined on A as								
0.	" aRb iff a and b have the		iation is defined on as	Tollows.							
			a) Tuon sitivo	d) Equivalence							
7	a) Reflexive	•	c) Transitive	d) Equivalence							
7.			e set of all trapeziums, the								
0	a) <i>P</i>	b) <i>T</i>	c) φ	d) None of these							
8.			proper subset of B . If $n(A)$	= 5, then find the minimum							
	possible value of $n(A\Delta \Delta A)$	В)									
	a) Is 1										
	b) Is 5										
	c) Cannot be determin	ed									
	d) None of these										
9.		$n(A \times B \times C) = 240$, the									
	a) 288	b) 1	c) 12	d) 2							
10.	In a class, 70 students wrote two tests viz;test-I and test-II. 50% of the students failed in test-I and 40% of the students in test-II. How many students passed in both tests?										
	the students in test-II.										
	a) 21	b) 7	c) 28	d) 14							
11.				$a, b \in \mathbb{Z}$ and $B = \{(a, b): a >$							
	$b, a, b \in \mathbb{Z}$. Then, the n	number of elements in A	$\cap B$ is								
	a) 2	b) 3	c) 4	d) 6							
12.	Let L be the set of all straight lines in the Euclidean plane. Two lines l_1 and l_2 are said to be related by the										
	relation R iff l_1 is paral	lel to l_2 . Then, the relati	on R is not								
	a) Reflexive	b) Symmetric	c) Transitive	d) None of these							
13.	Let <i>R</i> be a relation on t	he set N be defined by {	$((x,y) x,y\in N,2\;x+y=$	41}. Then, <i>R</i> is							
	a) Reflexive	b) Symmetric	c) Transitive	d) None of these							
14.	In an office, every emp	loyee likes at least one o	of tea, coffee and milk. The	number of employees who like							
	only tea, only coffee, or	nly milk and all the three	e are all equal. The numbe	er of employees who like only tea							
	and coffee, only coffee	and milk and only tea a	nd milk are equal and each	n is equal to the number of							
	-	-	=	employees in the office is							
	a) 65	b) 90	c) 77	d) 85							
15.		•	of elements in the power s	•							
	a) 26	b) 32	c) 8	d) 16							
	,	,	<i>)</i> -	•							

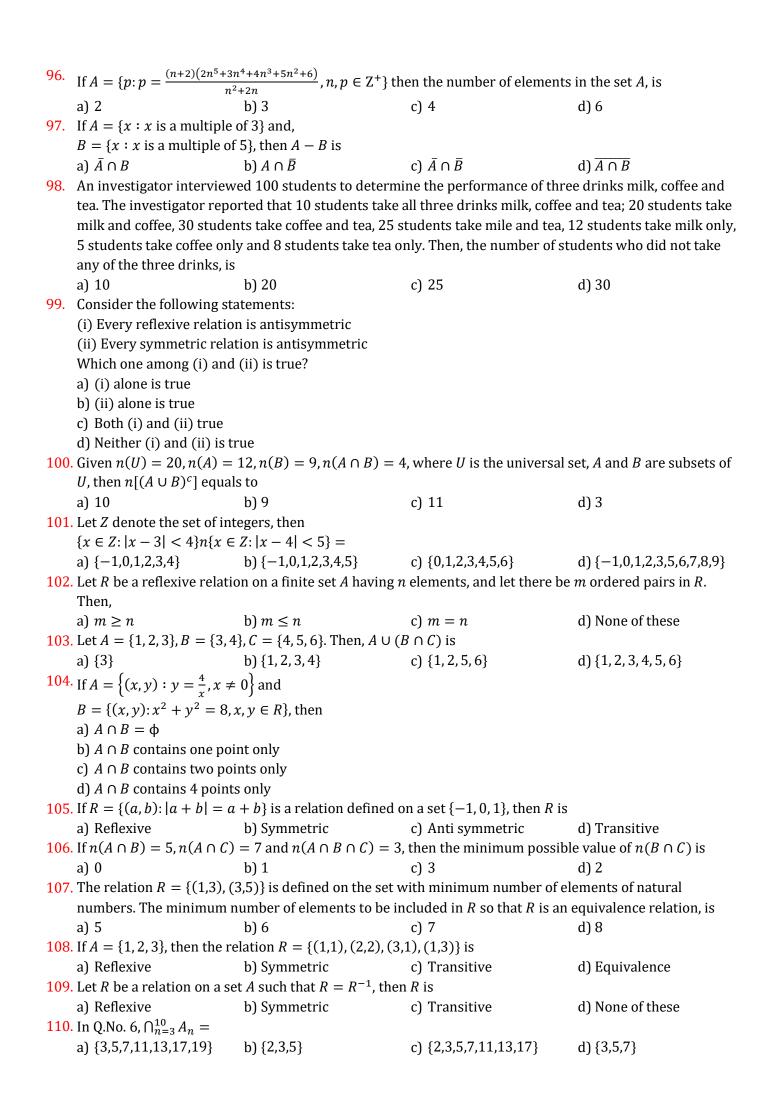
16.	The relation 'is subset of'	on the power set $P(A)$ of a	set A is								
	a) Symmetric	b) Anti-symmetric	c) Equivalence relation	d) None of these							
17.	Let <i>A</i> and <i>B</i> be two non-e	mpty subsets of a set <i>X</i> suc	h that A is not a subset of B	. Then,							
a) A is a subset of complement of B											
	b) <i>B</i> is a subset of <i>A</i>										
	c) Aand B are disjoint										
	d) A and the complement	of B are non-disjoint									
18.	If A, B and C are three set		$(A \cup B \cup C) - (A \cap B \cap C)$								
	a) $A - B$	b) $B-C$		d) None of these							
19.	A survey shows that 63% of the Americans like cheese whereas 76% like apples. If x % of the Americans like both cheese and apples, then										
			a) 20 < 4 < C2	d) Nama of these							
20	=	N) and $Y = \{9(n-1): n \in$	c) $39 \le x \le 63$	d) None of these							
20.	a) X	b) Y	c) N	d) None of these							
21	,	,	Itiple of 5}. Then, $A \cap B$ is gi								
21.		b) $\{5, 10, 15, 20, \dots \}$		d) None of these							
22	If $n(A \times B) = 45$, then $n($		() {13, 30, 43,}	u) None of these							
22.	a) 15	b) 17	c) 5	d) 9							
23	•	•	t A is an equivalence relation								
25.	a) Is reflective	defined on a non-empty se	e 11 13 an equivalence relatio	ii, it is sufficient, if it							
	b) Is symmetric										
	c) Is transitive										
	d) Possesses all the above	three properties									
24.	=		$\sqrt{2}$ is an irrational number.	Then, the relation R is							
	a) Reflexive	b) Symmetric		d) None of these							
25.		, ,	can speak English only. The	•							
	can speak both Hindi and	-	1 0 7	,							
	a) 9	b) 11	c) 23	d) 17							
26.	A, B and C are three non-	empty sets. If $A \subset B$ and B	$\subset C$, then which of the follo	wing is true?							
		b) $A \cap B \cap C = B$	c) $A \cup B = B \cap C$	$d) A \cup B \cup C = A$							
27.	$\left\{ x \in R : \frac{2x-1}{x^3+4x^2+3x} \in R \right\} eq^{-1}$	ıals									
	(x 11x 15x)) D (O 1 2)	n (1 1)							
			c) $R - \{0, -1, -3\}$								
28.		-	ts to a finite set B having n	elements, then the number							
	of relations from A to B is			15 10							
00	a) 2^{mn}	b) $2^{mn} - 1$	c) 2 <i>mn</i>	d) <i>m</i> ⁿ							
29.	If $A = \{(x, y): y^2 = x; x, y\}$										
	$B = \{(x, y): y = x ; x, y \in \mathbb{R} \}$	$\{R\}$, then									
	a) $A \cap B = \emptyset$										
	b) $A \cap B$ is a singleton set c) $A \cap B$ contains two ele										
	d) $A \cap B$ contains two ele	<u>-</u>									
30	Which of the following is	•									
50.	a) Is father of	b) Is less than	c) Is congruent to	d) Is an uncle of							
31.	•	=	cs, Physics and Chemistry,								
	-		matics and Physics, at most	=							
		-	nemistry. The largest possib	-							
	passed all three examinat	= -	, 51								
	a) 11	b) 12	c) 13	d) 14							
32.	Let <i>A</i> be the non-void set	of the children in a family.	The relation $'x$ is a brother	of y' on A is							

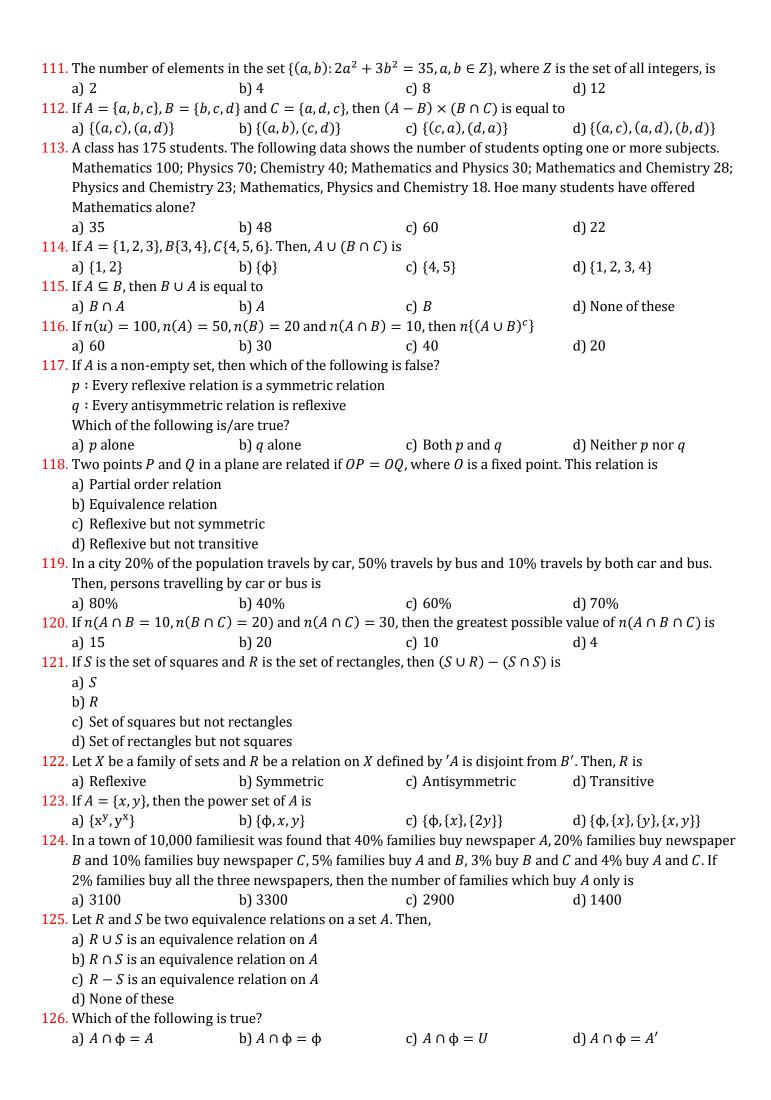
) D G :	13.0) m	12.34 ()								
	a) Reflexive	b) Symmetric	•	d) None of these								
33.	. In a class of 30 pupils 12 take needls work, 16 take physics and 18 take history. If all the 30 students take											
		o one takes all three, then t										
	a) 16	b) 6	c) 8	d) 20								
34.	34. If R is a relation on a finite set having n elements, then the number of relations on A is											
	a) 2 ⁿ	b) 2 ^{n²}	c) n^2	d) n^n								
35.	The void relation on a set	Ais										
	a) Reflexive											
b) Symmetric and transitive												
	c) Reflexive and symmetric											
	d) Reflexive and transitive											
36.	Suppose $A_1, A_2,, A_{30}$ are	thirty sets, each having 5 e	elements and B_1, B_2, \dots, B_n a	are n sets each with 3								
	elements, let											
	$\bigcup_{i=1}^{30} A_i = \bigcup_{j=1}^n B_j = S$ and	d each element of S belongs	to exactly 10 of the A_i 's an	d exactly 9 of the B_i 's.								
	Then, <i>n</i> is equal to			•								
	a) 115	b) 83	c) 45	d) None of these								
37.	If <i>A</i> is a finite set having <i>n</i>	•	,	,								
	a) 2 <i>n</i> elements	` ,	c) <i>n</i> elements	d) None of these								
38.	•	elements respectively. Wha		•								
	a) 3	b) 6	c) 9	d) 18								
39.		on on a set A and I be the identity		-, -								
	a) $R \subset I$	b) $I \subset R$	c) $R = I$	d) None of these								
40.		such that $n(A_i) = i + 2, A_1$		•								
	a) 3	b) 4	c) 5	d) 6								
41	•	sets, then $A \cap (A \cap B)^c$ is eq	•	a) o								
11.	a) A	b) <i>B</i>	с) Ф	d) $A \cap B^c$								
42.	•	R is a reflexive relation R	•	u)11112								
12.	a) $13 \le n \le 26$		c) $13 \le n \le 169$	d) $0 \le n \le 169$								
43.	•	ineering colleges in a state (=	•								
10.												
two colleges are related iff they are affiliated to the same university, then <i>R</i> is a) Only reflexive b) Only symmetric c) Only transitive d) Equivalent												
44	, ,	e number of families which	•	a) Equivalence								
	a) 4000	b) 3300	c) 4200	d) 5000								
45.	If <i>A</i> and <i>B</i> are two sets, th	,	c) 1200	u) 5000								
10.	a) A	b) <i>B</i>	c) ф	d) None of these								
46.		$A = \{2,4,18\}$ and $N = \{2,4,18\}$	•	•								
10.	a) A	b) <i>N</i>	c) B	d) none of these								
47.	If $A = \{\phi, \{\phi\}\}\$, then the p	•	c, <i>b</i>	a) hone of these								
17.			2) (4 (4) ((4)) 4)	d) None of these								
40	a) A	b) $\{\phi, \{\phi\}, A\}$	c) $\{\phi, \{\phi\}, \{\{\phi\}\}, A\}$	u) None of these								
48.	Let $A = \{(x, y) : y = e^x, x = e^x \}$	-										
	$B = \{(x, y) : y = e^{-x}, x \in \mathbb{R} \}$		3.4BB2	D.M. Col								
40	a) $A \cap B = \emptyset$		c) $A \cup B = R^2$	d) None of these								
49.		straight lines in a plane. Le	t a relation R be defined by	$\alpha R \beta \Leftrightarrow \alpha \perp \beta, \alpha, \beta \in L.$								
	Then R is	12.0										
	a) Reflexive	b) Symmetric	c) Transitive	d) None of these								
50.		s such that $A \cap B = A \cap Ca$		D 4 D								
	a) $A = C$	b) $B = C$	c) $A \cap B = \emptyset$	d) A = B								
51.		tal number of unordered pa										
	a) 25	b) 34	c) 42	d) 41								
52.	If $A = \{(x, y): x^2 + y^2 = 4\}$	$\{x, y \in R\}$ and										

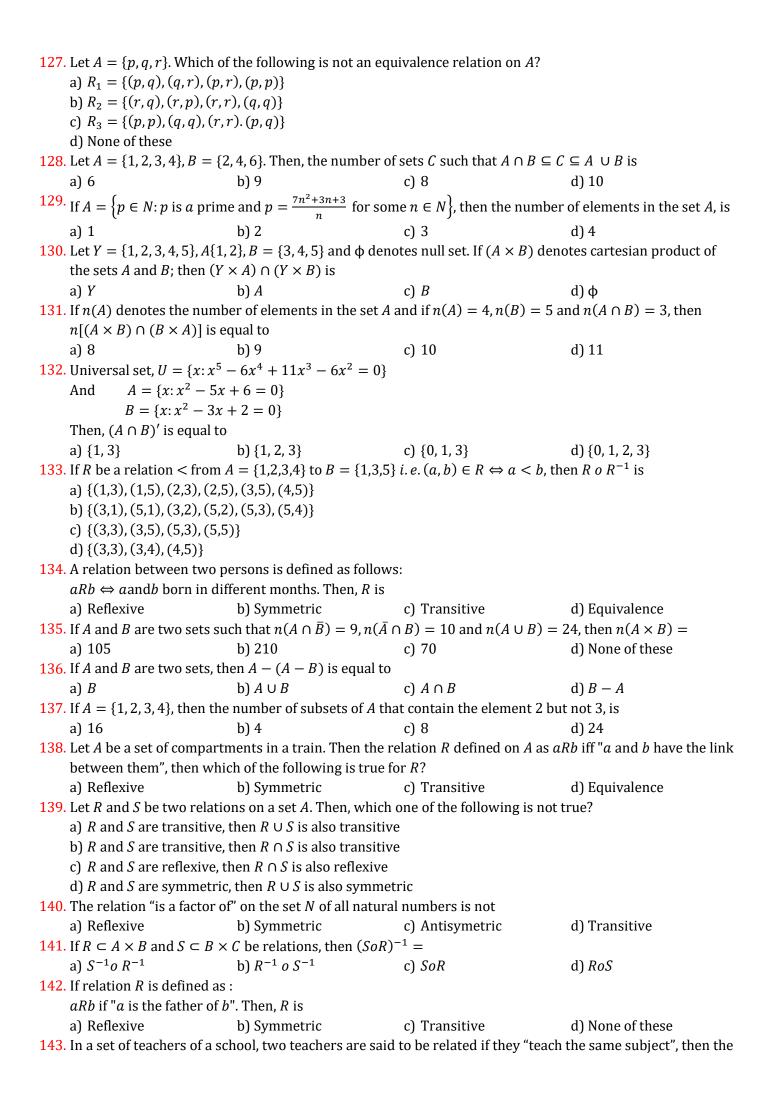


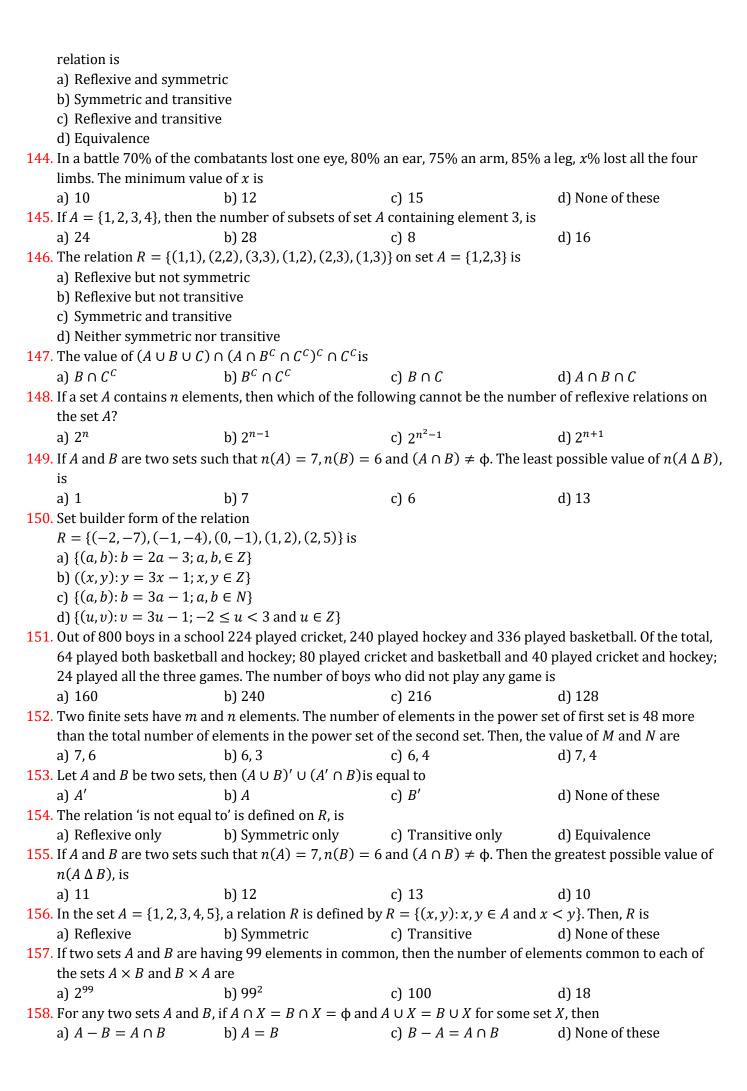


	a) Reflexive	b) Symmetric	c) Antisymmetric	d) Transitive							
84.	The shaded region in the	e figure represents									
	a) $A \cap B$	b) <i>A</i> ∪ <i>B</i>	c) $B-A$	$d) (A - B) \cup (B - A)$							
85.	Let $X = \{1, 2, 3, 4, 5\}$ and $Y = \{1, 3, 5, 7, 9\}$. Which of the following is/are not relations from X to Y ?										
	a) $R_1 = \{(x, y) y = 2 + x, x \in X, y \in Y\}$										
	b) $R_2 = \{(1,1), (2,1), (3,3), (4,3), (5,5)\}$										
c) $R_3 = \{(1,1), (1,3), (3,5), (3,7), (5,7)\}$											
	d) $R_4 = \{(1,3), (2,5$, , , ,									
86.	6. Given the relation $R = \{(1,2), (2,3)\}$ on the set $A = \{1,2,3\}$, the minimum number of ordered pairs which										
		t an equivalence relation is	\ -	1) 0							
07	a) 5	b) 6	c) 7	d) 8							
87.	If sets A and B are define										
	$A = \left\{ (x, y) \colon y = \frac{1}{x}, 0 \neq x \in R \right\},$										
	$B=\{(x,y)\colon y=-x,x\in$										
	•	b) $A \cap B = B$	•	d) None of these							
88.		relation on a finite set A hav	ring n elements. Then, the n	number of ordered pairs in							
	R is										
	a) Less than n	t o m									
	b) Greater than or equal to										
	c) Less than or equal tod) None of these	п									
89.	•	A_{50} and $n(A_i) = i - 1$, then	$n(\cap^{50}, A_i) =$								
03.	a) 49	b) 50	c) 11	d) 10							
90.	•	$\operatorname{id} b N \cap c N = d N, \text{ where } b$	•	u) 10							
		b) $c = bd$	c) $b = cd$	d) None of these							
91.	X is the set of all residents in a colony and R is a relation defined on X as follows:										
	"Two persons are relate	d iff they speak the same lan	guage"								
	The relation R is										
	a) Only symmetric										
	b) Only reflexive										
		reflexive but not transitive									
02	d) Equivalence	onto and $A = \{(a, a), a, a, c\}$	C as -t as) there the recomber	of alamanta in Aia							
92.	a) 100	ents and $A = \{(x, y) : x, y \in S \}$ b) 90	$(x \neq y)$, then the number $(x \neq y)$	d) 45							
03		AIL, GAIL, IOCL} and R be a r	•	•							
75.	they share exactly one le	•	ciation acmica as two cic.	ments of 11 are related if							
	a) Anti-symmetric	b) Only transitive	c) Only symmetric	d) Equivalence							
94.	•	have m and n elements respe									
		f subsets of B , then the volur									
	a) 7	b) 9	c) 10	d) 12							
95.	Let $R = \{(a, a)\}$ be a relative	ation on a set A . Then, R is									
	a) Symmetric										
	b) Antisymmetric										
	c) Symmetric and antisy										
	d) Neither symmetric nor antisymmetric										









159.	Which one of the followin	g relations on R is an equiv	alence relation?							
	a) $a R_1 b \Leftrightarrow a = b $	b) $a R_2 b \Leftrightarrow a \ge b$	c) $a R_3 b \Leftrightarrow a \text{ divides } b$	d) $a R_4 b \Leftrightarrow a < b$						
160.	Let <i>R</i> be a relation defined	d on <i>S</i> , the set of squares or	a chess board such that <i>xl</i>	Ry iff x and y share a						
	common side. Then, which of the following is false for <i>R</i> ?									
	a) Reflexive	b) Symmetric	c) Transitive	d) All the above						
161.	If $A = \{x, y, z\}$, then the re	elation								
	$R = \{(x, x), (y, y), (z, z), (z, z),$	(z,x),(z,y) is								
	a) Symmetric	b) Antisymmetric	c) Transitive	d) Both (a) and (b)						
162.	If $A = \{x : x \text{ is a multiple } c$	of 4} and,								
	$B = \{x : x \text{ is a multiple of } \}$	6}, then $A \cap B$ consists of r	nultiples of							
	a) 16	b) 12	c) 8	d) 4						
163.	If $A = \{a, b, c, l, m, n\}$, then	n the maximum number of	elements in any relation on	A is						
	a) 12	b) 16	c) 32	d) 36						
164.	Consider the following sta	atements:								
	<i>p</i> : Every reflexive relatio	n is symmetric relation								
	<i>q</i> : Every anti-symmetric	relation is reflexive								
	Which of the following is,	are true?								
	a) p alone	b) q alone	c) Both p and q	d) Neither <i>p</i> nor <i>q</i>						
165.	For any two sets <i>A</i> and <i>B</i> ,	A - (A - B) equals								
	a) <i>A</i>		c) <i>A</i> ∩ <i>B</i>	d) $A^C \cap B^C$						
166.	If A, B and C are three nor	n-empty sets such that A an	dB are disjoint and the nu	mber of elements						
	contained in <i>A</i> is equal to	those contained in the set of	of elements common to the	sets A and C, then $n(A \cup$						
	$B \cup C$) is necessarily equa	al to								
	a) $n(B \cup C)$	b) $n(A \cup C)$	c) Both (a) and (b)	d) None of these						
167.	The relation R defined in	N as $a R b \Leftrightarrow b$ is divisible	by a is							
	a) Reflexive but not symn	netric								
	b) Symmetric but not tran	ısitive								
	c) Symmetric and transiti	ve								
	d) None of these									
168.	If $A = \{n : \frac{n^3 + 5n^2 + 2}{n} \text{ is an in} \}$	nteger and itself is an intege	er) then the number of eler	nents in the set A is						
		L) 2) 2	1) 4						
1.00	a) 1	b) 2	c) 3	d) 4						
169.		the following data shows the	-	,						
	-	<u>=</u>		ematics and Chemistry 28;						
		; Mathematics, Physics and	Chemistry 18. How many	students have offered						
	Mathematics alone?	1.) 40	-) (0	1) 22						
150	a) 35	b) 48	c) 60	d) 22						
1/0.				be the subset of A consisting						
		ralue 1. Let C be the subset	of the set of all determinan	ts with value -1 . Then						
	a) <i>C</i> is empty	C								
	b) <i>B</i> has as many element	s as c								
	c) $A = B \cup C$									
171	d) B has twice as many electrical $B = B = C(x, y) \ln^2 x + y^2$									
1/1.	Let $P = \{(x, y) x^2 + y^2 = x\}$		a) Turan all l	J) A., 41						
	a) Reflexive	b) Symmetric	c) Transitive	d) Antisymmetric						

1 **(b)**

For any $a \in R$, we have $a \ge a$ Therefore, the relation R is reflexive.

R is not symmetric as $(2,1) \in R$ but $(1,2) \notin R$. The relation R is transitive also, because $(a,b) \in R$, $(b,c) \in R$ imply that $a \ge b$ and $b \ge c$ which in turn imply that $a \ge c$

2 **(d**)

Clearly, R is an equivalence relation

3 **(c)**

Let M and E denote the sets of students who have taken Mathematics and Economics respectively.

Then, we have

$$n(M \cup E) = 35, n(M) = 17 \text{ and } n(M \cap E') = 10$$

Now,

$$n(M \cap E') = n(M) - n(M \cap E)$$

$$\Rightarrow 10 = 17 - n(M \cap E) \Rightarrow n(M \cap E) = 7$$

Now,

$$n(M \cup E) = n(M) + n(E) - n(M \cap E)$$

$$\Rightarrow 35 = 17 + n(E) - 7 \Rightarrow n(E) = 25$$

$$n(E \cap M') = n(E) - n(E \cap M) = 25 - 7 = 18$$

4 (a)

Let
$$A = \{n(n+1)(2n+1): n \in Z\}$$

Putting
$$n = \pm 1, \pm 2, \dots$$
, we get $A = \{\dots - 1\}$

$$30, -6, 0, 6, 30, \dots$$

$$\Rightarrow \qquad \{n(n+1)(2n+1): n \in Z\} \subset \{6k: k \in Z\}$$

5 **(a)**

$$A \cup B = \{1, 2, 3, 4, 5, 6\}$$

$$\therefore (A \cup B) \cap C = \{1, 2, 3, 4, 5, 6\} \cap \{3, 4, 6\}$$

 $= \{3, 4, 6\}$

6 **(d)**

We have,

$$n(A \cap \overline{B}) = 9, n(\overline{A} \cap B) = 10$$
 and $n(A \cup B) = 24$

$$\Rightarrow n(A) - n(A \cap B) = 9, n(B) - n(A \cap B) = 10$$

and,
$$n(A) + n(B) - n(A \cap B) = 24$$

$$\Rightarrow n(A) + n(B) - 2n(A \cap B) = 19$$
 and $n(A) +$

$$n(B) - n(A \cap B) = 24$$

$$\Rightarrow n(A \cap B) = 5$$

$$\therefore n(A) = 14 \text{ and } n(B) = 15$$

Hence, $n(A \times B) = 14 \times 15 = 210$

7 **(a)**

Clearly, $P \subset T$

$$\therefore P \cap T = P$$

8 **(a)**

It is given that *A* is a proper subset of *B*

$$\therefore A - B = \phi \Rightarrow n(A - B) = 0$$

We have, n(A) = 5. So, minimum number of elements in B is 6

Hence, the minimum possible value of $n(A \Delta B)$ is n(B) - n(A) = 6 - 5 = 1

:

$$n(A \times B \times C) = n(A) \times n(B) \times n(C)$$

$$n(C) = \frac{24}{4 \times 3} = 2$$

10 **(b)**

Use $n(A \cup B) = n(A) + n(B) - n(A \cap B)$

11 **(d)**

$$A = \{(a,b): a^2 + 3b^2 = 28, a, b \in Z\}$$

$$=$$
{ $(5, 1), (-5, -1), (5, -1), (-5, 1), (1, 3), (-1, -3), (-1, 3),$

$$(1, -3), (4, 2), (-4, -2), (4, -2), (-4, 2)$$

And
$$B = \{(a, b): a > b, a, b \in Z\}$$

$$\therefore A \cap B$$

$$= \{(-1, -5), (1, -5), (-1, -3), (1, -3), (4, 2), (4, -1)\}$$

 \therefore Number of elements in $A \cap B$ is 6.

13 **(d)**

We have

$$R = \{(1,39), (2,37), (3,35), (4,33), (5,31), (6,29), \}$$

$$(7,27), (8,25), (9,23), (10,21), (11,19), (12,17),$$

(19,3),(20,1)

Since $(1,39) \in R$, but $(39,1) \notin R$

Therefore, *R* is not symmetric

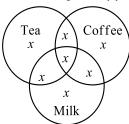
Clearly, R is not reflexive. Now, $(15,11) \in R$ and

 $(11,19) \in R$ but $(15,19) \notin R$

So, *R* is not transitive

14 **(c)**

Total number of employees = 7x i.e. a multiple of 7. Hence, option (c) is correct



15 **(a)**

The power set of a set containing n elements has 2^n elements.

Clearly, 2^n cannot be equal to 26

16 **(b)**

The relation is not symmetric, because $A \subset B$ does not imply that $B \subset A$. But, it is antisymmetric because

$$A \subset B$$
 and $B \subset A \Rightarrow A = B$

18 **(c)**

We have, $A \supset B \supset C$

$$\therefore A \cup B \cup C = A \text{ and } A \cap B \cap C = C$$

$$\Rightarrow (A \cup B \cup C) - (A \cap B \cap C) = A - C$$

19 **(c)**

Given, n(C) = 63, n(A) = 76 and $n(C \cap A) = x$ We know that,

$$n(C \cup A) = n(C) + n(A) - n(C \cap A)$$

⇒
$$100 = 63 + 76 - x$$
 ⇒ $x = 139 - 100 = 39$
And $n(C \cap A) \le n(C)$

Allu $n(C \cap A) \leq n(C)$

$$\Rightarrow x \leq 63$$

$$\therefore 39 \le x \le 63$$

20 **(b)**

We have,

X =Set of some multiple of 9

and, Y = Set of all multiple of 9

$$\therefore X \subset Y \Rightarrow X \cup Y = Y$$

21 **(c)**

 $A \cap B$

= $\{x: x \text{ a multiple of 3}\}$ and $\{x: x \text{ is a multiple of 5}\}$

= $\{x: x \text{ is a multiple of } 15\}$

$$= \{15, 30, 45, \dots \}$$

22 **(b)**

We have,

$$n(A \times B) = 45$$

$$\Rightarrow n(A) \times n(B) = 45$$

 \Rightarrow n(A) and n(B) are factors of 45 such that their product is 45

Hence, n(A) cannot be 17

24 **(a)**

For any $x \in R$, we have

$$x - x + \sqrt{2} = \sqrt{2}$$
 an irrational number

 $\Rightarrow x R x \text{ for all } x$

So, R is reflexive

R is not symmetric, because $\sqrt{2}$ *R* 1 but 1 $R / \sqrt{2}$ *R* is not transitive also because $\sqrt{2}$ *R* 1 and

$$1 R 2 \sqrt{2}$$
 but $\sqrt{2} R 2 \sqrt{2}$

25 **(b)**

We have,

$$n(H) - n(H \cap E) = 22, n(E) - n(H \cap E)$$

= 12, $n(H \cup E) = 45$

$$\therefore n(H \cup E) = n(H) + n(E) - n(H \cap E)$$

$$\Rightarrow 45 = 22 + 12 + n(H \cup E)$$

 $\Rightarrow n(H \cap E) = 11$

26 **(c)**

We have, $A \subset B$ and $B \subset C$

$$\therefore A \cup B = B \text{ and } B \cap C = B$$

$$\Rightarrow A \cup B = B \cap C$$

27 **(c)**

Let
$$A = \left\{ x \in R : \frac{2x-1}{x^3+4x^2+3x} \right\}$$

Now, $x^3 + 4x^2 + 3x = x(x^2 + 4x + 3)$
 $= x(x+3)(x+1)$

$$A = R - \{0, -1, -3\}$$

29 **(d)**

Clearly, $y^2 = x$ and y = |x| intersect at (0,0), (1,1) and (-1,-1). Hence, option (d) is correct

31 **(d)**

Let *M*, *P* and *C* be the sets of students taking examinations in Mathematics, Physics and Chemistry respectively.

We have.

$$n(M \cup P \cup C) = 50, n(M) = 37, n(P) = 24, n(C)$$

- 43

 $n(M \cap P) < 19, n(M \cap C) \le 29, n(P \cap C) \le 20$ Now,

$$n(M \cup P \cup C) = n(M) + n(P) + n(C) - n(M \cap P)$$

$$-n(M\cap C)-n(P\cap C)+n\ (M\cap P\cap C)$$

$$\Rightarrow 50 = 37 + 24 + 43 - \{n(M \cap P) + n(M \cap C) + n(P \cap C)\}\$$

 $+n(M \cap P \cap C)$

 $\Rightarrow n(M \cap P \cap C)$

$$= n(M \cap P) + n(M \cap C) + n(P \cap C) - 54$$

$$\Rightarrow n(M \cap P) + n(M \cap C) + n(P \cap C)$$

$$= n(M \cap P \cap C) + 54 \qquad \dots (i)$$

Now.

$$n(M \cap P) \le 19, n(M \cap C) \le 29, n(P \cap C) \le 20$$

$$\Rightarrow n(M \cap P) + n(M \cap C) + n(P \cap C) \le 19 + 29 + 10$$

$$\Rightarrow n(M \cap P \cap C) + 54 \le 68$$

$$\Rightarrow n(M \cap P \cap C) + 34 \le$$
$$\Rightarrow n(M \cap P \cap C) \le 14$$

33 **(a)**

Given,
$$n(N) = 12$$
, $n(P) = 16$, $n(H) = 18$,

$$n(N \cup P \cup H) = 30$$

And $n(N \cap P \cap H) = 0$

Now,
$$n(N \cup P \cup H) = n(N) + n(P) + n(H)$$

$$-n(N \cap P) - n(P \cap H) - n(H \cap N)$$

 $+n(N \cap P \cap H)$

$$\Rightarrow n(N \cap P) + n(P \cap H) + n(H \cap N)$$

$$=(12+16+18)-30$$

$$= 46 - 30 = 16$$

35 **(b)**

The void relation R on A is not reflexive as $(a, a) \notin R$ for any $a \in A$. The void relation is symmetric and transitive

36 **(c)**

Given,
$$A$$
's are 30 sets with five elements each, so $\sum_{i=1}^{30} n(A_i) = 5 \times 30 = 150$...(i)

If the
$$m$$
 distinct elements in S and each elements

of *S* belongs to exactly 10 of the
$$A_i$$
's, then
$$\sum_{i=1}^{30} n(A_i) = 10m \qquad ...(ii)$$

From Eqs. (i) and (ii),
$$m = 15$$

Similarly, $\sum_{j=1}^{n} n(B_j) = 3n \text{ and } \sum_{j=1}^{n} n(B_j) = 9m$ $\therefore \qquad 3n = 9m$ $\Rightarrow \qquad n = \frac{9m}{2} = 3 \times 15 = 45$

38 **(b)**

 $A \cup B$ will contain minimum number of elements if $A \subset B$ and in that case, we have $n(A \cup B) = n(B) = 6$

40 **(c)**

It is given that $A_1 \subset A_2 \subset A_3 \subset \cdots \subset A_{100}$ $\therefore \bigcup_{i=3}^{100} A_i = A \Rightarrow A_3 = A \Rightarrow n(A) = n(A_3) = 3 + 2$ = 5

41 (d)

We have, $A \cap (A \cap B)^c = A \cap (A^c \cup B^c)$ $\Rightarrow A \cap (A \cap B)^c = (A \cap A^c) \cup (A \cap B^c)$ $\Rightarrow A \cap (A \cap B)^c = \phi \cup (A \cap B^c) = A \cap B^c$

42 **(c)**

Since *R* is a reflexive relation on *A*. $\therefore (a, a) \in R \text{ for all } a \in A$ $\Rightarrow n(A) \le n(R) \le n(A \times A) \Rightarrow 13 \le n(R) \le 169$

43 **(d)**

Clearly, R is reflexive symmetric and transitive. So, it is an equivalence relation

44 (a)

We have,

Required number of families

 $= n(A' \cap B' \cap C')$ $= n(A \cup B \cup C)'$ $= N - n(A \cup B \cup C)$ $= 10000 - \{n(A) + n(B) + n(C) - n(A \cap B)\}$ $-n(B \cap C) - n(A \cap C) + n(A \cap B \cap C)\}$ = 10000 - 4000 - 2000 - 1000 + 500 + 300 + 400 - 200 = 4000

45 (a)

We have, $A \subset A \cup B$ $\Rightarrow A \cap (A \cup B) = A$

46 **(b)**

We have, $(A \cup B) \cap B' = A$ $\therefore ((A \cup B) \cap B') \cup A' = A \cup A' = N$

48 **(b)**

The set A consists of all points on $y = e^x$ and the set B consists of points on $y = e^{-x}$, these two curves intersect at (0, 1). Hence, $A \cap B$ consists of a single point

50 **(b)**

Given, $A \cap B = A \cap C$ and $A \cup B = A \cup C$ $\Rightarrow B = C$

51 **(d)**

Required number

$$=\frac{3^4+1}{2}=41$$

52 **(b)**

Clearly, *A* is the set of all points on a circle with centre at the origin and radius 2 and *B* is the set of all points on a circle with centre at the origin and radius 3. The two circles do not intersect.

Therefore,

$$A \cap B = \phi \Rightarrow B - A = B$$

53 **(c)**

We have, $n(A^c \cap B^c)$ $= n\{(A \cup B)^c\}$ $= n(U) - n(A \cup B)$ $= n(U) - \{n(A) + n(B) - n(A \cap B)\}$ = 700 - (200 + 300 - 100) = 300

54 **(a)**

We have,

$$\cos \theta > -\frac{1}{2} \text{ and } 0 \le \theta \le \pi$$

$$\Rightarrow 0 \le \theta \le 2\pi/3 \text{ and } 0 \le \theta \le \pi$$

$$\Rightarrow 0 \le \theta \le \frac{2\pi}{3} \Rightarrow A = \{\theta : 0 \le \theta \le 2\pi/3\}$$

Also

$$\sin \theta > \frac{1}{2} \text{ and } \pi/3 \le \theta \le \pi$$

$$\Rightarrow \frac{\pi}{3} \le \theta \le \frac{5\pi}{6} \Rightarrow B = \left\{\theta : \frac{\pi}{3} \le \theta \le \frac{5\pi}{6}\right\}$$

$$\therefore A \cap B = \left\{\theta : \frac{\pi}{3} \le \theta \le \frac{2\pi}{3}\right\} \text{ and } A \cup B$$

$$= \left\{\theta : 0 \le \theta \le \frac{5\pi}{6}\right\}$$

55 **(d)**

Clearly, R is an equivalence relation

56 **(c)**Given, $A = \{1, 2, 3\}, B = \{a, b\}$ $A \times B$ $= \{(1, a), (1, b), (2, a), (2, b), (3, a), (3, b)\}$

57 **(b)**Clearly,

$$A_2 \subset A_3 \subset A_4 \subset \cdots \subset A_{10}$$

$$\therefore \bigcup_{n=2}^{10} A_n = A_{10} = \{2,3,5,7,11,13,17,19,23,29\}$$

58 **(c)**Clearly,

 $= \{(4,6), (4,10), (6,4), (10,4)(6,10), (10,6), (10,12)\}$

Clearly, R is symmetric $(6,10) \in R$ and $(10,12) \in R$ but $(6,12) \notin R$ So, R is not transitive Also, R is not reflexive

61 **(c)**

It is given that

$$A_1 \subset A_2 \subset A_3 \dots \subset A_{99}$$

$$\bigcup_{i=1}^{999} A_i = A_{99}$$

$$\Rightarrow n\left(\bigcup_{i=1}^{99} A_i\right) = n(A_{99}) = 99 + 1 = 100$$

62 **(b)**

It is given that $2^m - 2^n = 56$

Obviously, m = 6, n = 3 satisfy the equation

63 **(b**)

Clearly, $(a, a) \in R$ for any $a \in A$ Also,

 $(a,b) \in R$

 \Rightarrow a and b are in different zoological parks

 \Rightarrow *b* and *a* are in different zoological parks

 \Rightarrow $(b,a) \in R$

Now, $(a, b) \in R$ and $(b, a) \in R$ but $(a, a) \notin R$ So, R is not transitive

64 **(d)**

$$X \cap Y = \{1, 2, 4, 5, 8, 10, 20, 25, 40, 50, 100, 200\}$$

$$\therefore \qquad n(X \cap Y) = 12$$

66 **(c)**

We have,

$$X \cap (Y \cup X)' = X \cap (Y' \cap X') = (X \cap X') \cap Y'$$
$$= \phi \cap Y' = \phi$$

67 **(b)**

The number of subsets of *A* containing 2, 3 and 5 is same as the number of subsets of set $\{1, 4, 6\}$ which is equal to $2^3 = 8$

68 **(a)**

We have,

$$B_1 = A_1 \Rightarrow B_1 \subset A_1$$

$$B_2 = A_2 - A_1 \Rightarrow B_2 \subset A_2$$

$$B_3 = A_3 - (A_1 \cup A_2) \Rightarrow B_3 \subset A_3$$

 $\therefore B_1 \cup B_2 \cup B_3 \subset A_1 \cup A_2 \cup A_3$

69 **(d)**

The identity relation on a set *A* is reflexive and symmetric both. So, there is always a reflexive and symmetric relation on a set

70 (a)

Let the total number of voters be n. Then, Number of voters voted for $A = \frac{nx}{100}$ Number of voters voted for $B = \frac{n(x+20)}{100}$: Number of voters who voted for both

$$= \frac{nx}{100} + \frac{n(x+20)}{100}$$

$$= \frac{n(2x+20)}{100}$$
Hence, $n - \frac{n(2x+20)}{100} = \frac{20n}{100} \Rightarrow x = 30$

71 **(c)**

Since $(1,1) \notin R$. So, R is not reflexive Now, $(1,2) \in R$ but, $(2,1) \notin R$. Therefore, R is not symmetric.

Clearly, R is transitive

72 **(b)**

Let *A* and *B* denote respectively the sets of families who got new houses and compensation It is given that

$$n(A \cap B) = n(\overline{A \cup B})$$

$$\Rightarrow n(A \cap B) = 50 - n(A \cup B)$$

$$\Rightarrow n(A) + n(B) = 50$$

$$\Rightarrow n(B) + 6 + n(B) = 50 \quad [\because n(A)$$

$$= n(B) + 6 \text{ (given)}]$$

$$\Rightarrow n(B) = 22 \Rightarrow n(A) = 28$$

73 **(b)**

We have,

$$n(A' \cap B') = n((A \cup B)')$$

$$\Rightarrow n(A' \cap B') = n(U) - n(A \cup B)$$

$$\Rightarrow n(A' \cap B') = n(U)$$

$$-\{n(A) + n(B) - n(A \cap B)\}\$$

$$\Rightarrow 300 = n(\mathcal{U}) - \{200 + 300 - 100\}$$
$$\Rightarrow n(\mathcal{U}) = 700$$

74 **(b)**

For any integer n, we have

 $n|n \Rightarrow n R n$

So, n R n for all $n \in Z$

 \Rightarrow *R* is reflexive

Now, 2|6 but 6 does not divide 2

 \Rightarrow (2, 6) \in R but (6,2) \notin R

So, *R* is not symmetric

Let $(m, n) \in R$ and $(n, p) \in R$. Then,

$$(m,n) \in R \Rightarrow m|n$$

 $(n,p) \in R \Rightarrow n|p$ $\Rightarrow m|p \Rightarrow (m,p) \in R$

So, *R* is transitive

Hence, *R* is reflexive and transitive but it is not symmetric

75 **(c)**

Since,
$$A = B \cap C$$
 and $B = C \cap A$,
Then $A \equiv B$

76 **(d)**

Since n|n for all $n \in N$. Therefore, R is reflexive. Since 2|6 but $6 \nmid 2$, therefore R is not symmetric Let $n \mid R \mid m$ and $m \mid R \mid p$ ⇒ n R m and m R p⇒ n|m and m|p ⇒ n|p ⇒ n R pSo, R is transitive

77 **(a)**

We have,

 $b \ N = \{b \ x | x \in \mathbb{N}\} = \text{Set of positive integral}$ multiples of b

 $c \ N = \{c \ x | x \in N\} = \text{Set positive integral}$ multiples of c

 $bN \cap cN = \text{Set of positive integral multiples of } bc$

 $\Rightarrow bN \cap cN = bc \ N \ [\because b \text{ and } c \text{ are prime}]$ Hence, d = bc

79 **(b)**

Let $x, y \in A$. Then, $x = m^2, y = n^2$ for some $m, n \in N$ $\Rightarrow xy = (mn)^2 \in A$

80 **(c)**

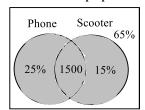
We have,

$$A_{1} \subset A_{2} \subset A_{3} \subset \dots \subset A_{100}$$

$$\therefore \bigcup_{i=1}^{100} A_{i} = A_{100} \Rightarrow n \left(\bigcup_{i=1}^{100} A_{i} \right) = n(A_{100}) = 101$$

81 **(c)**

Let the total population of town be x.



$$\therefore \frac{25x}{100} + \frac{15x}{100} - 1500 + \frac{65x}{100} = x$$

$$\Rightarrow \frac{105x}{100} - x = 1500$$

$$\Rightarrow \frac{5x}{100} = 1500$$

$$\Rightarrow x = 30000$$

82 **(d)**

As A, B, C are pair wise disjoints. Therefore, $A \cap B = \emptyset$, $B \cap C = \emptyset$ and $A \cap C = \emptyset$ $A \cap B \cap C = \emptyset$ $A \cap B \cap C \cap A \cap B \cap C$ $A \cap B \cap C \cap A \cap B \cap C$

83 **(b)**

Clearly, $R = \{(1,3), (3,1), (2,2)\}$ We observe that R is symmetric only

- 64 **(d)**Given figure clearly represents $(A B) \cup (B A)$
- 85 **(d)** R_4 is not a relation from A to B, because $(7,9) \in R_4$ but $(7,9) \notin A \times B$

86 **(c)**

R is reflexive if it contains (1,1), (2,2), (3,3) ∴ (1,2) ∈ R, (2,3) ∈ R ∴ R is symmetric, if (2,1), (3,2) ∈ R Now, $R = \{(1,1), (2,2), (3,3), (2,1), (3,2), (2,3), (1,2)\}$ R will be transitive, if (3,1), (1,3) ∈ R Thus, R becomes an equivalence relation by adding (1,1)(2,2)(3,3), (2,1)(3,2), (1,3), (3,1). Hence, the total number of ordered pairs is 7

87 **(c)**

The set A is the set of all points on the hyperbola xy=1 having its two branches in the first and third quadrants, while the set B is the set of all points on y=-x which lies in second and four quadrants. These two curves do not intersect. Hence, $A \cap B = \emptyset$.

88 **(b)**

Since R is an equivalence relation on set A. Therefore $(a, a) \in R$ for all $a \in A$. Hence, R has at least n ordered pairs

89 **(d**

It is given $A_1 \subset A_2 \subset A_3 \subset A_4 \dots \subset A_{50}$ $\therefore \bigcup_{i=11}^{50} A_i = A_{11}$ $\Rightarrow n \left(\bigcup_{i=11}^{50} A_i \right) = n(A_{11}) = 11 - 1 = 10$

90 **(d)**

We have,

 $b \ N = \{b \ x | x \in \mathbb{N}\} = \text{Set of positive integral}$ multiples of b

 $c \ N = \{c \ x | x \in N\} = \text{Set of positive integral}$ multiples of c

 $\therefore c \ N = \{c \ x \mid x \in N\} = \text{Set of positive integral}$ multiples of b and c both $\Rightarrow d = 1, c, m, of b \text{ and } c$

91 **(d)**

Clearly, R is an equivalence relation

92 **(b)**

Number of element is S = 10And $A = \{(x, y); x, y \in S, x \neq y\}$ \therefore Number of element in $A = 10 \times 9 = 90$

93 (c)

Clearly,

R = {(BHEL, SAIL), (SAIL, BHEL), (BHEL, GAIL), (GAIL, BHEL), (BHEL, IOCL), (IOCL, BHEL)}
We observe that R is symmetric only

94 **(a)**

According to the given condition,

$$2^{m} = 112 + 2^{n}$$

$$\Rightarrow 2^{m} - 2^{n} = 112$$

$$\Rightarrow m = 7, n = 4$$

96 **(c)**

We have,

$$p = \frac{(n+2)(2n^5 + 3n^4 + 4n^3 + 5n^2 + 6)}{n^2 + 2n}$$

$$\Rightarrow p = 2n^4 + 3n^3 + 4n^2 + 5n + \frac{6}{n}$$

Clearly, $p \in Z^+$ iff n = 1, 2, 3, 6. So, A has 4 elements

97 **(b)**

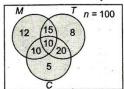
Clearly,

 $x \in A - B \Rightarrow x \in A \text{ but } x \notin B$

 \Rightarrow x is a multiple of 3 but it is not a multiple of 5 $\Rightarrow x \in A \cap \bar{B}$

98 **(b)**

Total drinks=3(ie, milk, coffee, tea).



Total number of students who take any of the drink is 80.

:The number of students who did not take any of three drinks = 100 - 80 = 20

100 (d)

$$n(A \cup B) = n(A) + n(B) - n(A \cap B)$$

= 12 + 9 - 4 = 17
Hence, $n[(AUB)^c] = n(U) - n(A \cup B)$

$$= 20 - 17 = 3$$

101 (c)

We have.

$$\{x \in Z: |x - 3| < 4\} = \{x \in Z: -1 < x < 7\}$$
$$= \{0.1, 2, 3, 4, 5, 6\}$$

$$\{x \in Z: |x - 4| < 5\} = \{x \in Z: -1 < x < 9\}$$

= \{0,1,2,3,4,5,6,7,8\}

$$\therefore \{x \in Z: |x - 3| < 4\} \cap \{x \in Z: |x - 4| < 5\}$$

$$= \{0,1,2,3,4,5,6\}$$

102 (a)

Since *R* is reflexive relation on *A*

 $(a, a) \in R$ for all $a \in A$

 \Rightarrow The minimum number of ordered pairs in R is n

Hence, $m \ge n$

104 (c)

We have, $y = \frac{4}{x}$ and $x^2 + y^2 = 8$

Solving these two equations, we have

$$x^2 + \frac{16}{x^2} = 8 \Rightarrow (x^2 - 4) = 0 \Rightarrow x = \pm 2$$

Substituting $x = \pm 2$ in $y = \frac{4}{r}$, we get $y = \pm 2$

Thus, the two curves intersect at two points only (2, 2) and (-2, 2). Hence, $A \cap B$ contains just two points

105 **(b)**

Let $(a, b) \in R$. Then,

$$|a+b| = a+b \Rightarrow |b+a| = b+a \Rightarrow (b,a) \in R$$

 $\Rightarrow R$ is symmetric

106 (c)

Minimum possible value of $n(B \cap C)$ is $n(A \cap B \cap C) = 3$

107 (a)

To make *R* a reflexive relation, we must have (1,1), (3,3) and (5,5) in it. In order to make R a symmetric relation, we must inside (3,1) and (5,3) in it.

Now, $(1,3) \in R$ and $(3,5) \in R$. So, to make R a transitive relation, we must have, $(1,5) \in R$. But, Rmust be symmetric also. So, it should also contain (5,1). Thus, we have

R

=
$$\{(1,1), (3,3), (5,5), (1,3), (3,5), (3,1), (5,3), (1,5),$$

Clearly, it is an equivalence relation on $A\{1,3,5\}$

108 **(b)**

Clearly, $(3,3) \notin R$. So, R is not reflexive. Also, (3,1)and (1,3) are in R but $(3,3) \notin R$. So, R is not transitive

But, *R* is symmetric as $R = R^{-1}$

109 **(b)**

Let $(a, b) \in R$. Then, $(a,b) \in R \Rightarrow (b,a) \in R^{-1}$ [By def. of R^{-1}] \Rightarrow $(b,a) \in R[\because R = R^{-1}]$ So, *R* is symmetric

110 **(b)**

We have,

$$A_2 \subset A_3 \subset A_4 \subset \cdots \subset A_{10}$$
$$\therefore \bigcap_{n=3}^{10} A_n = A_3 = \{2,3,5\}$$

111 (c)

The possible sets are
$$\{\pm 2, \pm 3\}$$
 and $\{\pm 4, \pm 1\}$; therefore, number of elements in required set is 8.

Given,
$$A = \{a, b, c\}$$
, $B = \{b, c, d\}$ and $C = \{a, d, c\}$
Now, $A - B = \{a, b, c\} - \{b, c, d\} = \{a\}$

Now,
$$A - B = \{a, b, c\} - \{b, c, d\} = \{a\}$$

And
$$B \cap C = \{b, c, d\} \cap \{a, d, c\} = \{c, d\}$$

$$\therefore (A - B) \times (B \cap C) = \{a\} \times \{c, d\}$$
$$= \{(a, c), (a, d)\}$$

Given,
$$n(M) = 100$$
, $n(P) = 70$, $n(C) = 40$
 $n(M \cap P) = 30$, $n(M \cap C) = 28$,
 $n(P \cap C) = 23$ and $n(M \cap P \cap C) = 18$
 $\therefore n(M \cap P' \cap C') = n[M \cap (P \cap C')]$
 $= n(M) - n[M \cap (P \cap C)]$
 $= n(M) - [n(M \cap P) + n(M \cap C) - n(M \cap P \cap C)]$
 $= 100 - [30 + 28 - 18 = 60]$

114 (d)

$$B \cap C = \{4\}.$$

$$A \cup (B \cap C) = \{1, 2, 3, 4\}$$

115 (c)

$$A \subseteq B$$

$$\therefore \qquad B \cup A = B$$

116 (c)

$$n((A \cup B)^c) = n(U) - n(A \cup B)$$

= $n(U) - \{n(A) + n(B) - n(A \cap B)\}$
= $100 - (50 + 20 - 10) = 40$

117 **(d)**

If
$$A = \{1,2,3\}$$
, then $R = \{(1,1), (2,2), (3,3), (1,2)\}$ is reflexive on A but it is not symmetric So, a reflexive relation need not be symmetric The relation 'is less than' on the set Z of integers

119 **(c)**

Clearly,

Required percent =
$$20 + 50 - 10 = 60\%$$

[: $n(A \cup B) = n(A) + n(B) - n(A \cap B)$]

is antisymmetric but it is not reflexive

120 **(c)**

The greatest possible value of $n(A \cap B \cap C)$ is the least amongst the values $n(A \cap B)$, $n(B \cap C)$ and $n(A \cap C)$ i.e. 10

121 **(d)**

Clearly, $S \subset R$

$$\therefore S \cup R = R \text{ and } S \cap R = S$$

 \Rightarrow $(S \cap R) - (S \cap R) = Set$ of rectangles which are not squares

122 **(b)**

Clearly, the relation is symmetric but it is neither reflexive nor transitive

123 **(d)**

Since, power set is a set of all possible subsets of a $\begin{vmatrix} 134 \end{vmatrix}$ (b)

$$P(A) = \{\phi, \{x\}, \{y\}, \{x, y\}\}$$

124 **(b)**

We have.

$$N = 10,000, n(A) = 40\% \text{ of } 10,000 = 4000,$$

 $n(B) = 2000, n(C) = 1000, n(A \cap B) = 500,$
 $n(B \cap C) = 300, n(C \cap A) = 400, n(A \cap B \cap C)$
 $= 200$

Now,

Required number of families =
$$n(A \cap \overline{B} \cap \overline{C}) = n(A \cap (B \cup C)')$$

= $n(A) - n(A \cap (B \cup C))$
= $n(A) - n((A \cap B) \cup (A \cap C))$
= $n(A) - \{n(A \cap B) + n(A \cap C) - n(A \cap B \cap C)\}$
= $4000 - (500 + 400 - 200) = 3300$

126 **(b)**

 $A \cap \phi = \phi$ is true.

128 (c)

$$A \cap B = \{2, 4\}$$

 $\{A \cap B\} \subseteq \{1, 2, 4\}, \{3, 2, 4\}, \{6, 2, 4\}, \{1, 3, 2, 4\}, \{1, 6, 2, 4\}, \{6, 3, 2, 4\}, \{2, 4\}, \{1, 3, 6, 2, 4\} \subseteq A \cup B$
 $\Rightarrow n(C) = 8$

129 **(a)**

We have,

$$p = \frac{7n^2 + 3n + 3}{n} \Rightarrow p = 7n + 3 + \frac{3}{n}$$

It is given that $n \in N$ and p is prime. Therefore,

$$n = 1$$

$$\therefore n(A) = 1$$

130 **(d)**

$$(Y \times A) = \{(1,1), (1,2), (2,1), (2,2), (3,1), (3,2), (4,1), (4,2), (5,1), (5,2)\}$$

And $(Y \times B) = \{(1,3), (1,4), (1,5), (2,3), (2,4), (2,5), (3,3), (3,4), (3,5), (4,3), (4,4), (4,5), (5,3), (5,4), (5,5)\}$
 $\therefore (Y \times A) \cap (Y \times B) = \emptyset$

131 **(b)**

Given,
$$n(A) = 4$$
, $n(B) = 5$ and $n(A \cap B) = 3$
 $\therefore n[(A \times B) \cap (B \times A)] = 3^2 = 9$

132 (c)

$$U = \{x: x^5 + 6x^4 + 11x^3 - 6x^2 = 0\} = \{0, 1, 2, 3\}$$

$$A = \{x: x^2 - 5x + 6 = 0\} = \{2, 3\}$$
And
$$B = \{x: x^2 - 3x + 2 = 0\} = \{2, 1\}$$

$$\therefore (A \cap B)' = U - (A \cap B)$$

$$= \{0, 1, 2, 3\} - \{2\} = \{0, 1, 3\}$$

133 **(c)**

We have,

$$R = \{(1,3), (1,5), (2,3), (2,5), (3,5), (4,5)\}$$

 $\Rightarrow R^{-1} = \{(3,1), (5,1), (3,2), (5,2), (5,3), (5,4)\}$
Hence, $R \circ R^{-1} = \{(3,3), (3,5), (5,3), (5,5)\}$

Let $(a, b) \in R$. Then,

a and b are born in different months \Rightarrow $(b, a) \in R$ So, *R* is symmetric

Clearly, *R* is neither reflexive nor transitive

136 (c)





From the venn diagram

$$A - (A - B) = A \cap B$$

137 **(b)**

Required number of subsets is equal to the number of subsets containing 2 and any number of elements from the remaining elements 1 and 4 So, required number of elements $= 2^2 = 4$

140 **(b)**

Clearly, 2 is a factor of 6 but 6 is not a factor of 2. So, the relation 'is factor of' is not symmetric. However, it is reflexive and transitive

142 (d)

Clearly, R is neither reflexive, nor symmetric and not transitive

143 (d)

Clearly, given relation is an equivalence relation

145 **(c)**

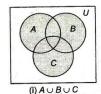
Each subset will contain 3 and any number of elements from the remaining 3 elements 1,2 and 4 So, required number of elements $= 2^2 = 8$

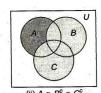
146 (a)

Since (1,1), (2,2), $(3,3) \in R$. Therefore, R is reflexive. We observe that $(1,2) \in R$ but $(2,1) \notin R$, therefore R is not symmetric.

It can be easily seen that *R* is transitive

147 **(b)**





GIII) C°

From figures (i), (ii) and (iii), we get $(A \cup B \cup C) \cap (A \cap B^C \cap C^C) \cap C^C = (B^C \cap C^C)$

148 (d)

A relation on set A is a subset of $A \times A$ Let $A = \{a_1, a_2, \dots, a_n\}$. Then, a reflexive relation on A must contain at least n elements $(a_1, a_1), (a_2, a_2), \dots, (a_n, a_n)$

∴ Number of reflexive relations on A is 2^{n^2-n} Clearly, $n^2 - n = n, n^2 - n = n - 1, n^2 - n = n^2 - 1$ have solutions in N but $n^2 - n = n + 1$ is not solvable in N.

So, 2^{n+1} cannot be the number of reflexive relations on A

149 **(a)**

We have,

$$A \Delta B = (A \cup B) - (A \cup B)$$

$$\Rightarrow n(A \Delta B) = n(A) + n(B) - 2 n(A \cap B)$$

So, $n(A \triangle B)$ is greatest when $n(A \cap B)$ is least It is given that $A \cap B \neq \phi$. So, least number of elements in $A \cap B$ can be one

∴ Greatest possible value of $n(A \triangle B)$ is 7 + 6 - 6

$$2 \times 1 = 11$$

150 **(d)**

Let
$$R = \{(x, y): y = ax + b\}$$
. Then,
 $(-2, -7), (-1, -4) \in R$
 $\Rightarrow -7 = -2a + b$ and $-4 = -a + b$
 $\Rightarrow a = 3, b = -1$
 $\therefore y = 3x - 1$
Hence, $R = \{(x, y): y = 3x - 1, -2 \le x < 3, x \in Z\}$

151 (a)

Let \mathcal{U} be the set of all students in the school. Let C, H and B denote the sets of students who played cricket, hockey and basketball respectively. Then, $n(\mathcal{U}) = 800, n(C) = 224, n(H) = 240, n(B)$

$$= 336$$
 $n(H \cap B) = 64, n(B \cap C) = 80, n(H \cap C) = 40$
and, $n(H \cap B \cap C) = 24$

∴Required number

$$= n(C' \cap H' \cap B')$$

$$= n(C \cup H \cup B)'$$

$$= n(\mathcal{U}) - n(\mathcal{C} \cup \mathcal{H} \cup \mathcal{B})$$

$$= n(\mathcal{U}) - \{n(C) + n(H) + n(B) - n(C \cap H) - n(H \cap B) - n(B \cap C) + n(C \cap H \cap B)\}$$

$$= 800 - \{224 + 240 + 336 + 336 - 64 - 80 - 40 + 24\}$$

$$= 800 - 640 = 160$$

152 (c)

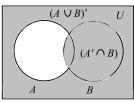
According to question,

$$2^m - 2^n = 48$$

This is possible only if m = 6 and n = 4.

153 (a)

From Venn-Euler's Diagram it is clear that



$$(A \cup B)' \cup (A' \cap B) = A'$$

154 **(b)**

For any $a, b \in R$

 $a \neq b \Rightarrow b \neq a \Rightarrow R$ is symmetric

Clearly, $2 \neq -3$ and $-3 \neq 2$, but 2 = 2. So, R is not transitive.

Clearly, R is not reflexive

155 (a)

We have,

$$A \Delta B = (A \cup B) - (A \cup B)$$

$$\Rightarrow n(A \Delta B) = n(A) + n(B) - 2 n(A \cap B)$$

So, $n(A \triangle B)$ is greatest when $n(A \cap B)$ is least It is given that $A \cap B \neq \phi$. So, least number of elements in $A \cap B$ can be one

 \therefore Greatest possible value of $n(A \triangle B)$ is 7 + 6 - $2 \times 1 = 11$

156 **(c)**

Since x < x, therefore R is not reflexive

Also, x < y does not imply that y < x

So *R* is not symmetric

Let x R y and y R z. Then, x < y and $y < z \Rightarrow x < y$

z i. e. x R z

Hence, R is transitive

157 **(b)**

Number of elements common to each set is 99 × $99 = 99^2$.

158 **(b)**

Given, $A \cap X = B \cap X = \phi$

 \Rightarrow AandX, B and X are disjoint sets.

 $A \cup X = B \cup X \Rightarrow A = B$

160 **(c)**

Clearly, *R* is reflexive and symmetric but it is not transitive

161 **(d)**

Clearly, R is an equivalence relation on A

162 **(b)**

Let $x \in A \cap B$. Then,

 $x \in A$ and $x \in B$

 \Rightarrow x is a multiple of 4 and x is a multiple of 6

 \Rightarrow x is a multiple of 4 and 6 both

 \Rightarrow x is a multiple of 12

163 **(d)**

Any relation on A is a subset of $A \times A$ which contains 36 elements. Hence, maximum number of elements in a relation on A can be 36

164 (d)

Clearly, none of the statements is true

165 (c)

Now,
$$A - (A - B) = A - (A - B^{C})$$

 $=A\cap (A\cap B^{\mathcal{C}})^{\mathcal{C}}$

 $=A\cap (A^C\cup B)$

 $= (A \cap A^C) \cup (A \cap B)$

 $= A \cap B$

166 (a)

We have,

$$A \cap B = \phi$$
 and $A \subset C$

$$\Rightarrow A \cap B = \phi$$
 and $A \cup C = C$

$$\therefore n(A \cup B \cup C) = n(A \cup C \cup B) = n(C \cup B)$$

$$= n(B \cup C)$$

167 (a)

For any $a \in N$, we have $a \mid a$

Therefore *R* is reflexive

R is not symmetric, because a R b does not imply

that b R a

168 **(d)**

$$\frac{n^3 + 5n^2 + 2}{n} = n^2 + 5n + \frac{2}{n}$$

 $\therefore \frac{n^3 + 5n^2 + 2}{n}$ is an integer, if $\frac{2}{n}$ is an integer

$$\Rightarrow n = \pm 1, \pm 2$$

 \Rightarrow A consists of four elements viz. -1, 1, -2, 2

169 (c)

We have,

$$c + e + f + g = 100$$

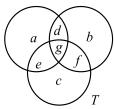
$$a + d + e + g = 70$$

$$b + d + f + g = 40$$

$$e + g = 30$$

$$g + f = 28$$

$$d + g = 23$$



$$g = 18$$

$$\therefore g = 18, f = 10, e = 12, d = 15, a = 35, b = 7, c$$
$$= 60$$

170 **(b)**

Since the value of a determinant charges by minus sign by interchanging any two rows or columns.

Therefore, corresponding to every element Δ of Bthere is an element Δ' in C obtained by

interchanging two adjacent rows (or columns) in Δ. It follows from this that $n(B) \le n(C)$

Similarly, we have $n(C) \leq n(B)$

Hence, n(B) = n(C)

171 **(b)**

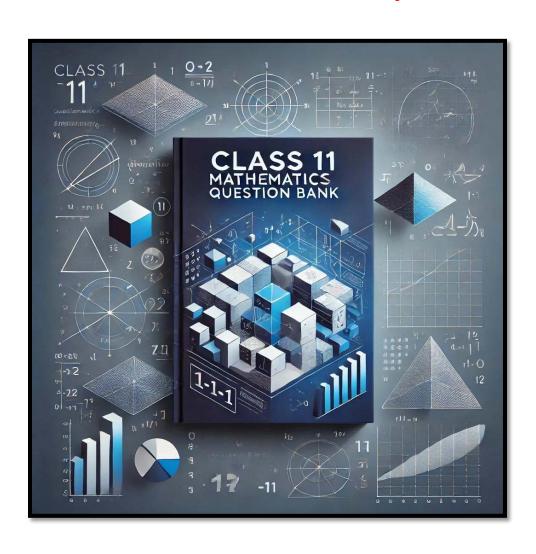
Obviously the relation is not reflexive and transitive but it is symmetric, because

$$x^2 + y^2 = 1 \Rightarrow y^2 + x^2 = 1$$

1)	b	2)	d	3)	c	4)	a	89)	d	90)	d	91)	d	92)	b
5)	a	6)	d	7)	a	8)	a	93)	c	94)	a	95)	c	96)	c
9)	d	10)	b	11)	d	12)	d	97)	b	98)	b	99)	d	100)	d
13)	d	14)	C	15)	a	16)	b	101)	c	102)	a	103)	b	104)	c
17)	d	18)	C	19)	c	20)	b	105)	b	106)	c	107)	a	108)	b
21)	c	22)	b	23)	d	24)	a	109)	b	110)	b	111)	c	112)	a
25)	b	26)	C	27)	c	28)	a	113)	c	114)	d	115)	c	116)	c
29)	d	30)	C	31)	d	32)	c	117)	d	118)	b	119)	c	120)	c
33)	a	34)	b	35)	b	36)	c	121)	d	122)	b	123)	d	124)	b
37)	b	38)	b	39)	b	40)	c	125)	b	126)	b	127)	d	128)	c
41)	d	42)	C	43)	d	44)	a	129)	a	130)	d	131)	b	132)	c
45)	a	46)	b	47)	c	48)	b	133)	C	134)	b	135)	b	136)	c
49)	b	50)	b	51)	d	52)	b	137)	b	138)	b	139)	a	140)	b
53)	C	54)	a	55)	d	56)	c	141)	b	142)	d	143)	d	144)	a
57)	b	58)	C	59)	a	60)	d	145)	c	146)	a	147)	b	148)	d
61)	C	62)	b	63)	b	64)	d	149)	a	150)	d	151)	a	152)	c
65)	C	66)	C	67)	b	68)	a	153)	a	154)	b	155)	a	156)	c
69)	d	70)	a	71)	c	72)	b	157)	b	158)	b	159)	a	160)	c
73)	b	74)	b	75)	c	76)	d	161)	d	162)	b	163)	d	164)	d
77)	a	78)	c	79)	b	80)	c	165)	c	166)	a	167)	a	168)	d
81)	c	82)	d	83)	b	84)	d	169)	c	170)	b	171)	b		
85)	d	86)	c	87)	c	88)	b								



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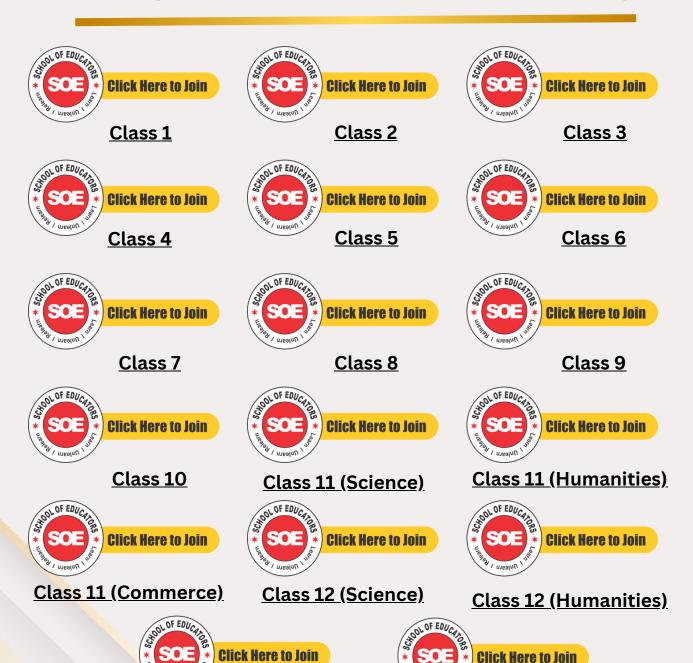
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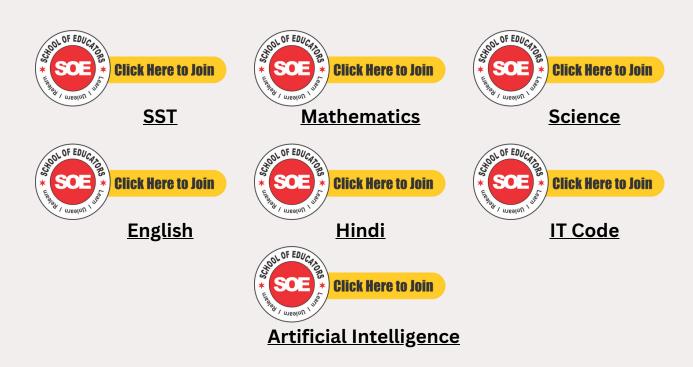
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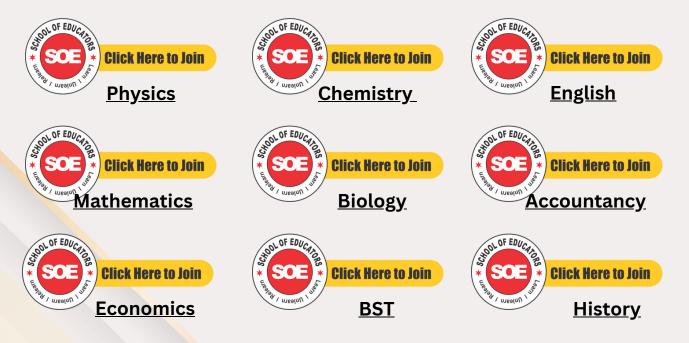




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What to do when Doctor is not around



Humanity & Covid-19



MAL More and Market Mar







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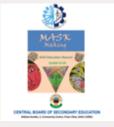
<u>Baking</u>



<u>Herbal Heritage</u>



<u>Khadi</u>



Mask Making



Mass Media



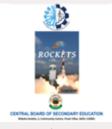
Making of a Graphic Novel



<u>Embroidery</u>



<u>Embroidery</u>



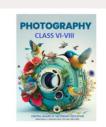
Rockets



Satellites



<u>Application of</u> <u>Satellites</u>



<u>Photography</u>

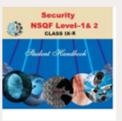
SKILL SUBJECTS AT SECONDARY LEVEL (CLASSES IX - X)



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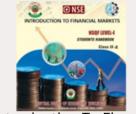
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Security



<u>Automotive</u>



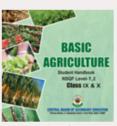
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Beauty & Wellness



Agriculture



Food Production



Front Office Operations



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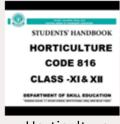


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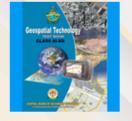
Insurance



Horticulture



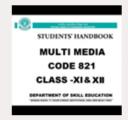
Typography & Comp. **Application**



Geospatial Technology



Electronic Technology



Multi-Media



Taxation



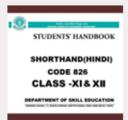
Cost Accounting



Office Procedures & Practices



Shorthand (English)



Shorthand (Hindi)



<u>Air-Conditioning &</u> <u>Refrigeration</u>



Medical Diagnostics



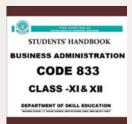
Textile Design



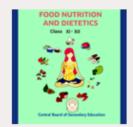
<u>Design</u>



<u>Salesmanship</u>



<u>Business</u> Administration



Food Nutrition & Dietetics



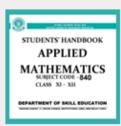
Mass Media Studies



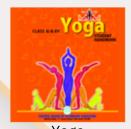
<u>Library & Information</u> Science



Fashion Studies



Applied Mathematics



<u>Yoga</u>



<u>Early Childhood Care &</u> <u>Education</u>



<u>Artificial Intelligence</u>



Data Science



Physical Activity
Trainer(new)



<u>Land Transportation</u>
<u>Associate (NEW)</u>



Electronics & Hardware (NEW)



<u>Design Thinking &</u> <u>Innovation (NEW)</u>

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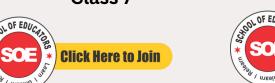


















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Class 12 (Science)

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Class 8







Class 10





Class 12 (Humanities)



Artifical intelligence

Subject Wise Secondary and Senior Secondary Groups IX & X

Secondary Groups (IX & X)









Hindi-A



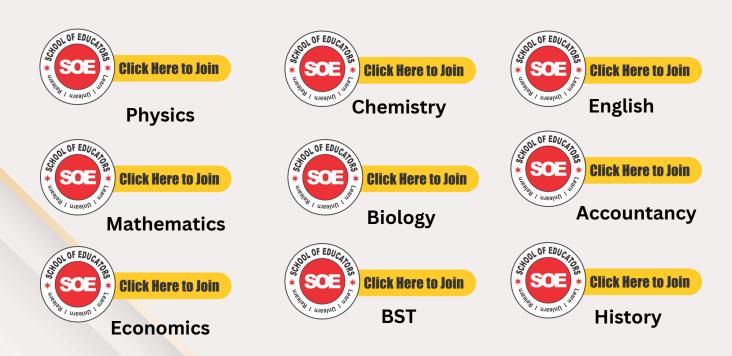
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